

# 1 xNet+SC: Classifying Places Based on Images by 2 Incorporating Spatial Contexts

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## 16 — Abstract —

17 With recent advancements in deep convolutional neural networks, researchers in geographic in-  
18 formation science gained access to powerful models to address challenging problems such as  
19 extracting objects from satellite imagery. However, as the underlying techniques are essentially  
20 borrowed from other research fields, e.g., computer vision or machine translation, they are often  
21 not spatially explicit. In this paper, we demonstrate how utilizing the rich information embedded  
22 in spatial contexts (SC) can substantially improve the classification of place types from images  
23 of their facades and interiors. By experimenting with different types of spatial contexts, namely  
24 spatial relatedness, spatial co-location, and spatial sequence pattern, we improve the accuracy  
25 of state-of-the-art models such as ResNet – which are known to outperform humans on the Im-  
26 ageNet dataset – by over 40%. Our study raises awareness for leveraging spatial contexts and  
27 domain knowledge in general in advancing deep learning models, thereby also demonstrating that  
28 theory-driven and data-driven approaches are mutually beneficial.

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## 34 **1** Introduction

35 Recent advancements in computer vision models and algorithms have quickly permeated  
36 many research domains including GIScience. In remote sensing, computer vision methods  
37 facilitate researchers to utilize satellite images to detect geographic features and classify  
38 land use [5, 26]. In urban planning, researchers collect Google Street View images and  
39 apply computer vision algorithms to study urban change [22]. In cartography, pixel-wise  
40 segmentation has been adopted to extract lane boundary from satellite imagery [32] and deep  
41 convolutional neural network (CNN) has been utilized to recognize multi-digit house numbers  
42 from Google Street View images [10]. These recent breakthroughs in computer vision are



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43 achieved, in equal parts, due to advances in deep neural networks as well as the ever-increasing  
44 availability of extensive training datasets. For example, the classification error in the latest  
45 image classification challenge using the ImageNet dataset is down to about 0.023.<sup>1</sup>

46 However, such impressive results do not imply that these models have reached a level  
47 in which no further improvement is necessary or meaningful. On the contrary, such deep  
48 learning models which primarily depend on visual signals are susceptible to error. In fact,  
49 studies have shown that deep (convolutional) neural networks suffer from a lack of robustness  
50 to adversarial examples and a tendency towards biases [25]. Researchers have discovered that,  
51 by incorporating adversarial perturbations of inputs that are indistinguishable by humans,  
52 the most advanced deep learning models which have achieved high accuracy on test sets can  
53 be easily fooled [6, 11, 28]. In addition, deep learning models are also vulnerable to biased  
54 patterns learned from the available data and these biases usually resemble many unpleasant  
55 human behaviors in our society. For instance, modern neural information processing systems  
56 such as neural network language models and deep convolutional neural networks have been  
57 criticized for amplifying racial and gender biases [3, 4, 25, 33]. Such biases, which can  
58 be attributed to a discrepancy between the distribution of prototypical examples and the  
59 distribution of more complex real world systems [16], have already caused some public debates.  
60 To give a provocative example, almost three years after users revealed that Google erroneously  
61 labeled photos of black people as “gorillas”, no robust solutions have been established besides  
62 simply removing such labels for now.<sup>2</sup>

63 The above-mentioned drawbacks are being addressed by improvements to the available  
64 training data as well as the used methods [23, 3]. In our work, we follow this line of thought to  
65 help improve image classification. In our case, these images depict the facades or interiors of  
66 different types of places, such as restaurants, hotels, and libraries. Classifying images by place  
67 types is a hard problem in that more often than not the training image data is inadequate to  
68 provide a full visual representation of different place types. Solely relying on visual signals,  
69 as most deep convolutional neural networks do, falls short in modeling the feature space  
70 as a result. To give an intuitive example, facades of restaurants may vary substantially  
71 based on the type of restaurant, the target customers, and the surrounding. Their facade  
72 may be partially occluded by trees or cars, may be photographed from different angles and  
73 at different times of the day, and the image may contain parts of other buildings. Put  
74 differently, the principle of spatial heterogeneity implies that there is considerable variation  
75 between places of the same type.

76 To address this problem and improve classification accuracy, we propose to go beyond  
77 visual stimuli by incorporating spatial contextual information to help offset the visual  
78 representational inadequacy. Although data availability is less of an issue nowadays, the biased  
79 pattern in the data poses a real challenge, especially as models such as deep convolutional  
80 neural networks take a very long time to train. Instead of fine-tuning the parameters (weights)  
81 by collecting and labeling more unbiased data, which are very resource-consuming, we take  
82 advantage of external information, namely spatial context. There are many different ways  
83 one can model such context; in this work, we focus on the types of nearby places. We explore  
84 and compare the value of three different kinds of spatial context, namely spatial relatedness,  
85 spatial co-location, and spatial sequence pattern.

86 We combine these context models with state-of-the-art deep convolutional neural network  
87 models using search re-ranking algorithms and Bayesian methods. The result shows that,  
88 by considering more complex spatial contexts, we can improve the classification accuracy

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<sup>2</sup> <https://www.wired.com/story/when-it-comes-to-gorillas-google-photos-remains-blind/>

89 for different place types. In fact, our results demonstrate that a *spatially explicit* model  
90 [9], i.e., taking nearby places into account when predicting the place type from an image,  
91 improves the accuracy of leading image classification models by at least 40%. Aside from this  
92 substantial increase in accuracy, we believe that our work also contributes to the broader  
93 and ongoing discussion about the role of and need for theory, i.e., domain knowledge, in  
94 machine learning. Finally, and as indicated in the title, our spatial context (*SC*) models,  
95 can be added to any of the popular CNN-based computer vision models such as AlexNet,  
96 ResNet, and DenseNet – abbreviated to *xNet* here.

97 The remainder of this paper is organized as follows. Section 2 provides an overview of  
98 existing work on spatial context and methods for incorporating spatial information into  
99 image classification models. Section 3 presents the image classification tasks and provides  
100 information about the convolutional neural network models used in our study. Section 4  
101 explains in detail three different levels of spatial context and ways to combine them in image  
102 classification models. Section 5 presents the results. Finally, Section 6 concludes the research  
103 and points to future directions.

## 104 **2** Related Work

105 There is a large body of work that utilizes spatial context to improve existing methods and  
106 provide deeper insights into the rich semantics of contextual information more broadly. For  
107 instance, spatial context has been recognized as a complementary source of information in  
108 computational linguistics. By training word embeddings for different place types derived  
109 from OpenStreetMap (OSM) and Google Places, Cocos and Callison-Burch [7] suggested that  
110 spatial context provides useful information about semantic relatedness. In Points of Interest  
111 (POI) recommendation, spatial context has been used to provide latent representations of POI,  
112 to facilitate the prediction of future visitors [8], and to recommend similar places [34]. By  
113 implementing an information theoretic and distance-lagged augmented spatial context, Yan  
114 et al. [30] demonstrated that high-dimensional place type embeddings learned using spatial  
115 contexts can reproduce human-level similarity judgments with high accuracy. The study  
116 showed that such a spatially explicit Place2Vec model substantially outperforms Word2Vec-  
117 based models that utilize a linguistic-style of context. Liu et al. [21] used spatial contexts to  
118 measure traffic interactions in urban area. In object detection, Heitz and Koller [13] leveraged  
119 spatial contexts in a probabilistic model to improve detection result. Likewise, by embracing  
120 the idea that spatial context provides valuable extrinsic signals, our work analyzes different  
121 kinds of spatial contexts and tests their ability to improve image classification of place types.

122 Existing work on image classification has realized the importance of including a geographic  
123 component. One direction of research focused on enriching images with geospatial data.  
124 Baatz et al. [1] took advantage of digital elevation models to help geo-localize images in  
125 mountainous terrain. Lin et al. [20] made use of land cover survey data and learned the  
126 complex translation relationship between ground level images and overhead imagery to extend  
127 the reach of image geo-localization. Instead of estimating a precise geo-tag, Lee et al. [19]  
128 trained deep convolutional neural networks to enrich a photo with geographic attributes such  
129 as elevation and population density. Another direction of research (which is more similar to  
130 our study) focused on utilizing geographic information to facilitate image classification. In  
131 order to better understand scenes and improve object region recognition, Yu and Luo [31]  
132 exploited information from seasons and location proximity of images using a probabilistic  
133 graphical model. Berg et al. [2] combined one-vs-most image classifiers with spatiotemporal  
134 class priors to address the problem of distinguishing images of highly similar bird species.

135 Tang et al. [29] encoded geographic features extracted from GPS information of images into  
 136 convolutional neural networks to improve classification results.

137 Our work differs from the existing work in that we explicitly exploit the distributional  
 138 semantics found in spatial context [30] to improve image classification. Following the linguistic  
 139 mantra that one *shall know a word by the company it keeps*, we argue that one can know  
 140 a place type by its neighborhood’s types. This raises the interesting question of how such  
 141 a neighborhood should be defined. We will demonstrate different ways in which spatial  
 142 contextual signals and visual signals can be combined. We will assess to what extent different  
 143 kinds of spatial context, namely spatial relatedness, spatial co-location, and spatial sequence  
 144 pattern, can provide such neighborhood information to benefit image classification.

### 145 **3 Image Classification**

146 In this section, we first describe the image classification task and the data we use. The task is  
 147 similar to scene classification but we are specifically interested in classifying different business  
 148 venues as opposed to natural environment. Then we explain four different deep convolutional  
 149 neural networks that solely leverages the visual signals of images. These convolutional neural  
 150 network models are later used as baselines for our experiment.

#### 151 **3.1 Classification Task**

152 Our task is to classify images into one of the several candidate place types. Because we want  
 153 to utilize the spatial context in which the image was taken, we need to make sure each image  
 154 has a geographic identifier, e.g. geographic coordinates, so that we are able to determine its  
 155 neighboring place and their types. In order to classify place types of images, we consider  
 156 the scene categories provided by Zhou et al. [35] as they also provide pretrained models  
 157 (Places365-CNN) that we can directly use.<sup>3</sup> Without losing generality, we select 15 place  
 158 types as our candidate class labels. The full list of class labels and their alignment with the  
 159 categories in Places365-CNN is shown in Table 1. For each candidate class, we selected 50  
 160 images taken in 8 states<sup>4</sup> within the US by using Google Maps, Google Street View, and  
 161 Yelp. These images include both indoor and outdoor views of each place type. Please note  
 162 that classifying place types from facade and interior images is a hard problem and even the  
 163 most sophisticated models only distinguish a relatively small number of place types so far  
 164 which is nowhere near the approximately 420 types provided by sources such as Foursquare.  
 165 Places365, for instance, offers 365 classes but many of these are scenes or landscape features,  
 166 such as waves, and not POI type, such as cinemas, in the classical sense.

#### 167 **3.2 Convolutional Neural Network Models**

168 To establish baselines for our study, we selected several state-of-the-art image classification  
 169 models, namely deep convolutional neural networks. Unlike traditional image classification  
 170 pipelines, CNNs extract features from images automatically based on the error messages that  
 171 are backpropagated through the network, thus fewer heuristics and less manual labor are  
 172 needed. Contrary to densely connected feedforward neural networks, CNN adopts parameter  
 173 sharing to extract common patterns which help capture translation invariance and creates  
 174 sparse connections which result in fewer parameters and being less prone to overfitting.

<sup>3</sup> [https://github.com/CSAILVision/places365/blob/master/categories\\_places365.txt](https://github.com/CSAILVision/places365/blob/master/categories_places365.txt)

<sup>4</sup> Arizona, Illinois, Nevada, North Carolina, Ohio, Pennsylvania, South Carolina, and Wisconsin

■ **Table 1** Class label alignment between Yelp and the Places365 model.

Class label	Places365-CNN category
Amusement Parks	amusement_park
Bakeries	bakery
Bookstores	bookstore
Churches	church
Cinema	movie_theater
Dance Clubs	discotheque
Drugstores	drugstore, pharmacy
Hospitals	hospital, hospital_room
Hotels	hotel, hotel_room
Jewelry	jewelry_shop
Libraries	library
Museums	museum, natural_history_museum, science_museum
Restaurants	fastfood_restaurant, restaurant, restaurant_kitchen, restaurant_patio
Shoe Stores	shoe_shop
Stadiums & Arenas	stadium

175 The architecture of CNNs has been revised numerous times and has become increasingly  
 176 sophisticated since its first appearance about 30 years ago. These improvements in architecture  
 177 have made CNN more powerful as can be seen in the ImageNet challenge. Some of the  
 178 notable architectures include: LeNet [18], AlexNet [17], VGG [24], Inception [27], ResNet  
 179 [12], and DenseNet [15]. We selected AlexNet, ResNet with 18 layers (ResNet18), ResNet  
 180 with 50 layers (ResNet50), and DenseNet with 161 layers (DenseNet161). AlexNet is among  
 181 the first deep neural networks that increased the classification accuracy on ImageNet by  
 182 a significant amount compared with traditional classification approaches. By using skip  
 183 connections to create residual blocks in the network, ResNet makes it easy to learn identity  
 184 functions that help with the vanishing and exploding gradient problems when the network  
 185 goes deeper. In DenseNet, a dense connectivity pattern is created by connecting every two  
 186 layers so that the error signal can be directly propagated to earlier layers, parameter and  
 187 computational efficiency can be increased, and low complexity features can be maintained  
 188 [15]. These models were trained on 1.8 million images from the Places365-CNN dataset. We  
 189 used the pretrained weights for these models.

## 190 **4 Spatial Contextual Information**

191 In this section, we introduce three different kinds of spatial contexts and explore ways in  
 192 which we can combine them with the CNN models in order to improve image classification.  
 193 The first type of spatial context is spatial relatedness, which measures the extend to which  
 194 different place types relate with each other. The second type of spatial context is spatial  
 195 co-location, which considers what place types tend to co-occur in space and the frequency  
 196 they cluster with each other. The third type of spatial context is spatial sequence pattern  
 197 which considers both spatial relatedness and spatial co-location. In addition, spatial sequence  
 198 pattern considers the interaction between context place types and the inverse relationship  
 199 between distance and contextual influence. We use POIs provided by Yelp as dataset. <sup>5</sup>

<sup>5</sup> <https://www.yelp.com/dataset>

200 **4.1 Spatial Relatedness**

201 Since the output of CNN is the probability score for each class label, it is possible to interpret  
 202 our task as a ranking problem: given an image, rank the candidate class labels based upon  
 203 the visual signal and spatial context signal. For the visual signal, we can obtain the ranking  
 204 scores (probability scores) from the CNN architectures mentioned in Section 3. Since the  
 205 original CNN models has 365 labels, we renormalize the probability scores for each candidate  
 206 place type by the sum of the 15 candidate ranking scores so that they sum up to 1. This  
 207 renormalization procedure is also applied to the other two spatial context methods explained  
 208 in Section 4.2 and Section 4.3. We will refer to the renormalized scores as CNN scores in this  
 209 study. For the spatial context signal, the ranking scores are calculated using the place type  
 210 embeddings proposed in [30]. These embeddings capture the semantics of different place  
 211 types and can be used to measure their similarity and relatedness. In this regard, the task is  
 212 equivalent to a re-ranking problem, which adjusts the initial ranking provided by the visual  
 213 signal using auxiliary knowledge, namely the spatial context signal. Intuitively, the extent  
 214 to which the visual signals from the images match with different place types and the level  
 215 of relevance of the surrounding place types with respect to candidate place types jointly  
 216 determine the final result.

217 Inspired by search re-ranking algorithms in information retrieval, we use a *Linear Bimodal*  
 218 *Fusion* (LBF) method (here essentially a 2-component convex combination), which linearly  
 219 combines the ranking scores provided by the CNN model and the spatial relatedness scores,  
 220 as shown in Equation 1.

$$221 \quad s_i = \omega^v s_i^v + \omega^r s_i^r \quad (1)$$

222 where  $s_i$ ,  $s_i^v$ , and  $s_i^r$  are the LBF score, CNN score, and spatial relatedness score for place  
 223 type  $i$  respectively,  $\omega^v$  and  $\omega^r$  are the weights for the CNN component and spatial relatedness  
 224 component, and  $\omega^v + \omega^r = 1$ . The weights here are decided based on the relative performance  
 225 of individual components. Specifically, the weight is determined using Equation 2.

$$226 \quad \omega^v = \frac{acc^v}{acc^v + acc^r} \quad (2)$$

227 where  $acc^v$  and  $acc^r$  are the accuracies for CNN and spatial relatedness measurements for  
 228 the image classification task. Intuitively, this means that we have higher confidence if the  
 229 component performs better on its own and want to reflect such confidence using the weight  
 230 in the LBF score.

231 In order to calculate the spatial relatedness scores, we use cosine similarity to measure  
 232 the extend to which each candidate class embedding is related with the spatial context  
 233 embedding of an image in a high dimensional geospatial semantic feature space. Following  
 234 the suggestions in [30], we use a concatenated vector of 350 dimensions (i.e., 70D vectors for  
 235 each of 5 distance bins) as the place type embeddings. The candidate class embeddings can  
 236 be retrieved directly. Then we search for the nearest  $n$  POIs based on the image location,  
 237 determine the place types of these  $n$  POIs, and calculate the average of these place type  
 238 embeddings as the final spatial context embeddings for images. The cosine similarity score  
 239  $sm_i$  is calculated between the spatial context embedding of an image and the embedding  
 240 of each candidate place type class  $i$ . Because  $sm_i$  ranges from -1 to 1, we use min-max  
 241 normalization to scale the values to  $[0, 1]$ . Finally, we apply the same renormalization as for  
 242 the CNN score to turn the normalized score  $sm_i$  into probability score, i.e. spatial relatedness  
 243 score  $s_i^r$ .

244 Combining these normalizations together with Equation 1 and Equation 2, we are able to  
 245 derive that  $0 \leq s_i \leq 1$  and  $\sum_{i=1}^N s_i = 1$  where  $N = 15$  in our case. This means that the LBF  
 246 score  $s_i$  can be considered a probability score.

## 247 4.2 Spatial Co-location

248 The spatial relatedness approach follows the assumption that relatedness implies likelihood  
 249 which is reasonable in cases where similar place types cluster together, such as restaurant,  
 250 bar, and hotel. However, in cases of high spatial heterogeneity, this assumption will fall short  
 251 of correctly capturing the true likelihood. An example would be places of dissimilar types  
 252 that co-occur, e.g., grocery stores and gas stations. Moreover, the LBF method can only  
 253 capture a linear relationship between the two signals.

254 Following Berg et al.[2], we also test a Bayesian approach in which we assume there is a  
 255 complex latent distribution of the data that facilitates our classification task. Intuitively,  
 256 the CNN score gives us the probability of each candidate class  $t$  given the image  $I$ , i.e.,  
 257  $P(t|I)$ , and the spatial context informs us of the probability of each candidate class given its  
 258 neighbors  $c_1, c_2, c_3, \dots, c_n$ , denoted as  $C$ , around the image location, i.e.,  $P(t|C)$ . We would  
 259 like to obtain the posterior probability of each candidate class given both the image and  
 260 its spatial context, i.e.,  $P(t|I, C)$ . Using Bayes' theorem, the posterior probability can be  
 261 written as:

$$262 \quad P(t|I, C) = \frac{P(I, C|t)P(t)}{P(I, C)} \quad (3)$$

263 For variables  $I$ ,  $C$ , and  $t$ , we construct their dependencies using a simple probabilistic  
 264 graphical model, i.e., Bayesian network, which assumes that both the image  $I$  and the spatial  
 265 context  $C$  are dependent on the place type  $t$ , which intuitively makes sense in that different  
 266 place types will result in different images and different place types of their neighbors. We  
 267 know that given information about the image  $I$  we are able to update our beliefs, i.e., the  
 268 probability distributions, about the place type  $t$ . In addition, the changes in our beliefs about  
 269 the place type  $t$  can influence the probability distributions of the spatial context  $C$ . However,  
 270 if place type  $t$  is observed, the influence cannot flow between  $I$  and  $C$ , thus we are able to  
 271 derive the conditional independence of  $I$  and  $C$  given  $t$ . So Equation 3 can be rewritten as:

$$272 \quad \begin{aligned} P(t|I, C) &= \frac{P(I|t)P(C|t)P(t)}{P(I, C)} \\ &= \frac{P(t|I)P(I)}{P(t)} \frac{P(t|C)P(C)}{P(t)} \frac{P(t)}{P(I, C)} \\ &\propto \frac{P(t|I)}{P(t)} P(t|C) \end{aligned} \quad (4)$$

273 in which we have dropped all the factors that are not dependent on  $t$  as they can be considered  
 274 as normalizing constants for our probabilities. It follows that the posterior probability  
 275  $P(t|I, C)$  can be computed using the CNN probability score  $P(t|I)$ , the spatial context prior  
 276  $P(t|C)$ , and the candidate class prior  $P(t)$ . Instead of estimating the distribution of spatial  
 277 context priors, we take advantage of the spatial co-location patterns and calculate the prior  
 278 probabilities using the Yelp POI data directly. As mentioned earlier, the spatial context  
 279  $C$  is composed of multiple individual context neighbors  $c_1, c_2, c_3, \dots, c_n$ ; hence, we need to  
 280 calculate  $P(t|c_1, c_2, c_3, \dots, c_n)$ . In order to simplify our calculation, we impose a bag-of-words  
 281 assumption as well as a Naive Bayes assumption in the spatial co-location patterns. The  
 282 bag-of-words assumption simplifies the model by assuming that the position (or the order) in

283 which different context POIs occur does not play a role. The Naive Bayes assumption implies  
 284 that the only relationship is the pair-wise interaction between the candidate place type  $t$   
 285 and an individual neighbor's place type  $c_i$  and there is no interaction between neighboring  
 286 places wrt. their types, i.e.  $(c_i \perp\!\!\!\perp c_j | t)$  for all  $c_i, c_j$ . Using spatial co-location, we are able to  
 287 calculate the conditional probability using place type co-location counts  $P(c_i | t) = \frac{\text{count}(c_i, t)}{\text{count}(t)}$   
 288 where  $\text{count}(c_i, t)$  is the frequency that neighbor type  $c_i$  and candidate type  $t$  co-locate  
 289 within a certain distance limit and  $\text{count}(t)$  is the frequency of candidate type  $t$  in the study  
 290 area. Combining all these components, we can derive:

$$\begin{aligned}
 P(t|C) &= P(t|c_1, c_2, \dots, c_n) \\
 &= \frac{P(t) \prod_{i=1}^n P(c_i|t)}{P(c_1, c_2, c_3, \dots, c_n)} \\
 &= \frac{P(t)}{P(c_1, c_2, c_3, \dots, c_n)} \frac{\prod_{i=1}^n \text{count}(c_i, t)}{\text{count}(t)^n}
 \end{aligned} \tag{5}$$

292 Using Equation 4 and Equation 5, we can derive the final formula for calculating  $P(t|I, C)$   
 293 shown in Equation 6. For the sake of numerical stability, we calculate the log probability  
 294  $\log P(t|I, C)$  using the natural logarithm. Since the natural logarithm is a monotonically  
 295 increasing function, it will not affect the final ranking of the classification results.

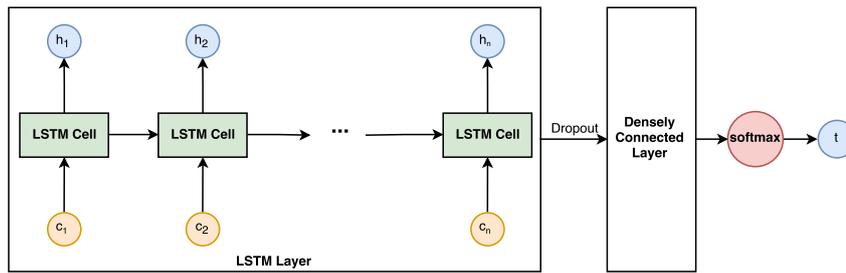
$$\begin{aligned}
 \log P(t|I, C) &\propto \log \left( \frac{P(t|I)}{P(t)} P(t|C) \right) \\
 &= \log \left( \frac{P(t|I)}{P(c_1, c_2, c_3, \dots, c_n)} \frac{\prod_{i=1}^n \text{count}(c_i, t)}{\text{count}(t)^n} \right) \\
 &\propto \log P(t|I) + \sum_{i=1}^n \log(\text{count}(c_i, t)) - n \log(\text{count}(t))
 \end{aligned} \tag{6}$$

297 where we also drop  $P(c_1, c_2, c_3, \dots, c_n)$  as it does not depend on  $t$ , so it will not affect the  
 298 result ranking. The log posterior probability is then used to generate the final ranking of  
 299 candidate place types and produce the classification results.

### 300 4.3 Spatial Sequence Pattern

301 The spatial co-location approach follows the bag-of-words assumption that the position of  
 302 spatial context POIs does not matter and the Naive Bayes assumption that the context  
 303 neighbors are independent of each other. However, in many cases this assumption is too  
 304 strong. In fact, numerous methods, such as Kriging and multiple-point geostatistics, have  
 305 been devised to model geospatial proximity patterns and complex spatial interaction patterns.  
 306 However, incorporating these complex spatial patterns in a multidimensional space would  
 307 adversely affect the model complexity and make the distribution in Section 4.2 intractable.  
 308 In order to strike the right balance between the complexity of model and the integrity of  
 309 spatial context pattern, we propose to capture the spatial sequence pattern in our model by  
 310 collapsing the 2D geographic space into a 1D sequence.

311 Specifically, we use the Long Short-Term Memory (LSTM) network model, a variant of  
 312 recurrent neural network (RNN), in our study. Recurrent neural networks are frequently  
 313 used models to capture the patterns in sequence or time series data. In theory, the naive  
 314 recurrent neural networks can capture long term dependencies in the sequence, however,  
 315 due to the vanishing and exploding gradient problem, they fail to do so in practice. LSTM  
 316 is explicitly designed to solve the problem by maintaining a cell state and controlling the



■ **Figure 1** Structure of the LSTM.

317 input and output flow using forget gate, input gate, and output gate [14]. We use LSTM  
 318 as a generative model in order to capture the latent distribution of place types using the  
 319 spatial sequence pattern. In the training stage, the input is a sequence of context place  
 320 types  $c_1, c_2, c_3, \dots, c_n$  and the output is the place type  $t$  of the POI from which the context is  
 321 created. The input sequence is ordered in a way so that the previous one is further away  
 322 from the output than the next one in the collapsed 1D space. Image one would drive around  
 323 a neighborhood before reaching a destination. For each of the POIs encountered during the  
 324 route, one would update the beliefs about the neighborhood by considering the current POI  
 325 and all previously seen POIs. Upon arriving at the destination, one would have a reasonable  
 326 chance of guessing this final POI's type. The structure of the LSTM model is shown in  
 327 Figure 1. We apply a dropout after the LSTM layer to avoid overfitting. After training  
 328 the LSTM model on Yelp's POI dataset, we are able to obtain the spatial context prior  
 329  $P(t|c_1, c_2, c_3, \dots, c_n)$  based on the spatial sequence pattern around the image locations in our  
 330 test data. We specifically removed the image locations and their context in the training data.  
 331 Similar to the spatial co-location approach, we use Bayesian inference and log probability to  
 332 calculate the final result:

$$\begin{aligned}
 \log P(t|I, C) &\propto \log \left( \frac{P(t|I)}{P(t)} P(t|C) \right) \\
 &= \log P(t|I) + \log P(t|c_1, c_2, c_3, \dots, c_n) - \log P(t)
 \end{aligned}
 \tag{7}$$

334 where the candidate class prior  $P(t)$  can be computed using the Yelp data. Since we use LSTM  
 335 as a generative model, in the prediction phase, sampling strategies, such as greedy search,  
 336 beam search, and random sampling, can be applied based on the distribution provided  
 337 by the output of the LSTM prediction. However, we only generate the next prediction  
 338 instead of a sequence, so we do not apply these sampling strategies. Instead, we make use of  
 339 the hyperparameter *temperature*  $\tau$  to adjust the probability scores returned by the LSTM  
 340 model before combining them with the CNN model in a Bayesian manner. Including the  
 341 hyperparameter  $\tau$ , the softmax function in the LSTM model can be written as:

$$P(t_i|C) = \frac{\exp(\frac{\text{logit}_i}{\tau})}{\sum_{j=1}^N \exp(\frac{\text{logit}_j}{\tau})}
 \tag{8}$$

343 where  $\text{logit}_i$  is the logit output provided by LSTM before applying the softmax function and  
 344  $N = 15$  in our case. Intuitively, when the temperature  $\tau$  is high, i.e.,  $\tau \rightarrow \infty$ , the probability  
 345 distribution will become diffuse and  $P(t_i|C)$  will have almost the same value for different  $t_i$ ;  
 346 when  $\tau$  is low, i.e.,  $\tau \rightarrow 0^+$ , the distribution becomes peaky and the largest  $\text{logit}_i$  stands  
 347 out to have a probability close to 1. This idea is closely related to the exploration and  
 348 exploitation trade-off in many machine learning problems. The value of  $\tau$  will affect the  
 349 probability scores  $P(t_i|C)$  but not the ranking of these probabilities.

350 In this study, we propose two ways to model the 2D geographic space as a 1D sequence.  
 351 The first one is a distance-based ordering approach. For any given POI, we search for nearby  
 352 POIs within a certain distance from it, choose the closest  $n$  POIs, and rearrange them by  
 353 distance with descending order, thereby forming a 1D array. This distance-based method is  
 354 isotropic in that it does not differentiate between directions while creating the sequence. The  
 355 second method is a space filling curve-based approach. We utilize *Morton order* here which  
 356 is also used in geohashing to encode coordinates into an indexing string that can preserve  
 357 the locality of spatial locations. We use Morton order to encode the geographic locations of  
 358 every POI and order them in a sequence based upon their encodings, i.e., indexing sequence.  
 359 After obtaining the sequence, for each POI, we use the previous  $n$  POI in the sequence as  
 360 the context sequence. Other space filling curves could be used in future work.

361 Because each POI can have multiple place types associated with it, e.g., restaurant and  
 362 beer garden, the sequence of place types is usually not unique for the same sequence of POIs.  
 363 As our LSTM input is a sequence of place *types*, we compute the Cartesian product of all  
 364 POI type sets in the sequence of nearby places:

$$365 \quad T_{c_1} \times T_{c_2} \times T_{c_3} \times \dots \times T_{c_n} = \{(t_{c_1}, t_{c_2}, t_{c_3}, \dots, t_{c_n}) | \forall i = 1, 2, 3, \dots, n, t_{c_i} \in T_{c_i}\} \quad (9)$$

366 where  $T_{c_i}$  is the set of place types associated with POI  $c_i$  in the context sequence. In  
 367 practice, however, we randomly sample a fixed number of place type sequences from each  
 368 of the Cartesian product for the POI context sequence as the potential combinations grow  
 369 exponentially with increasing context size.

## 370 **5 Experiment and Result**

371 In this section, we explain our experimental setup for the models described above, describe  
 372 the metrics used to compare the model performance for place type image classification, and  
 373 present the results and findings.

### 374 **5.1 Implementation Details**

375 For all three types of spatial context, we use 10 as the maximum number of context POIs  
 376 and a distance limit of 1000m for the context POI search. For the spatial sequence pattern  
 377 approach, we use a fixed sample size of 50 to sample from the Cartesian product of all POI  
 378 type sets in the sequence.<sup>6</sup> We use a one-layer LSTM with 64 hidden units. We train our  
 379 LSTM model using the recommended Root Mean Square Propagation (RMSProp) optimizer  
 380 with a learning rate of 0.005. A dropout ratio of 0.2 is applied in the LSTM and we run  
 381 100 epochs. The same settings are used for all LSTM trainings in our experiment. The  
 382 total number of POI in the dataset is 115,532, yielding more than 5 million unique training  
 383 sequences.

384 For evaluation, we use three different metrics, namely Mean Reciprocal Rank (MRR),  
 385 Accuracy@1, and Accuracy@5. Another common metric for image classification would also  
 386 be Mean Average Precision (MAP), but since there is only one true label per type in our  
 387 task, we use MMR instead.

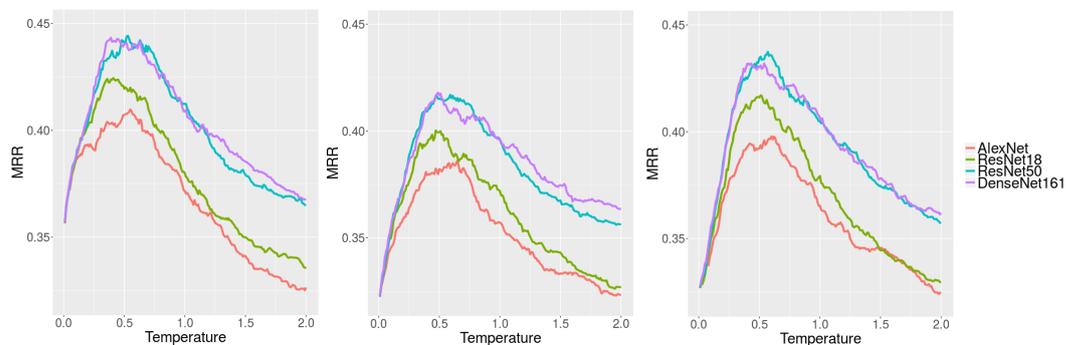
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<sup>6</sup> The median for types per place in Yelp is 3.

## 5.2 Results

We run the 750 test images we collected, i.e., 50 images per each of 15 types, on the four CNN baseline models (AlexNet, ResNet18, ResNet50, and DenseNet161) as well as the combined models using our three different types of spatial context.<sup>7</sup> In addition to the two methods for converting geographic space into 1D sequences in the spatial sequence pattern approach, we also test one model using random sequences with the same context count and distance limits. We did so to study whether results obtained using the LSTM would benefit from distance-based spatial contexts. A higher result for the spatial sequence based LSTM over the random LSTM would indicate that the network indeed picked up on the distance signal.

The hyperparameter  $\tau$  can be adjusted; a value of 0.5 has been proposed as a good choice before. In order to test this and find the optimal temperature value, we run the combined model using spatial sequence patterns with three types of sequencing approaches, namely random sequence, distance-based sequence, and Morton order-based sequence.



**Figure 2** From left to right, MRR result using distance-based sequence, random sequence, and Morton code-based sequence with varying temperatures

We test temperature values ranging from 0.01 to 2 with a step of 0.01. We combine the spatial sequence pattern models with all CNN models. The MRR result with respect to temperature are shown in Figure 2. Although there are slight variations, the MRR curves all reach their peaks around a  $\tau$  value of 0.5. This confirms the suggestion from the literature. Figure 3 shows selected example predictions. The results for MRR, Accuracy@1, and Accuracy@5 using the baseline models as well as our proposed, spatially explicit models are shown in Table 2, Table 3, and Table 4.<sup>8</sup>

As we can see, by incorporating spatial context in the image classification model, we are able to improve the classification result in general. However, integrating spatial relatedness using the LBF method does not seem to affect the result. This essentially confirms our aforementioned assumption that relatedness does not always imply likelihood. The benefit of incorporating spatial relatedness in cases of spatial homogeneity are likely to be offset by cases of high spatial heterogeneity in which spatial relatedness may have a negative effect as dissimilar places co-occur.

<sup>7</sup> Transfer learning could be applied to fine tune the CNN models first, but we only have limited images and our hypothesis is that spatial context can be used as a powerful complement or alternative to the visual component for image classification.

<sup>8</sup> The baseline models are not comparable with a random classifier which would yield an expected accuracy of 1/15 in this case, because the baseline CNN models have 365 unique labels and we choose 15 labels in our experiment.



■ **Figure 3** From left to right, images of a restaurant, a hotel, and a museum from Yelp, Google Street View, and Google Maps respectively. The first image is incorrectly classified as library using all 4 CNN models and it is correctly classified as restaurant using the spatial sequence pattern (distance) models. The second image is classified as hospital and library by the original CNN models and is classified as hotel by the spatial sequence pattern (distance) models. For the third image the correct label museum is in the third position in the label rankings of all 4 CNN models while, using the spatial sequence pattern (distance) models, ResNet18 and ResNet50 can correctly label it and in the label rankings of AlexNet and DenseNet161 museum is in the second position.

■ **Table 2** MRR result using baseline models and proposed combination models using different types of spatial context and sequences

MRR	AlexNet	ResNet18	ResNet50	DenseNet161
Baseline	0.27	0.28	0.31	0.31
Relatedness	0.27	0.28	0.31	0.32
Co-location	0.30	0.31	0.31	0.32
Sequence Pattern (Random)	0.38	0.40	0.42	0.42
Sequence Pattern (Distance)	<b>0.41</b>	<b>0.42</b>	<b>0.44</b>	<b>0.44</b>
Sequence Pattern (Morton order)	0.39	<b>0.42</b>	0.43	0.43

415 The Accuracy@1 measurement is improved by incorporating spatial co-location component  
 416 in the models. This confirms our previous reasoning that considering the external signal,  
 417 namely spatial contexts, and assuming a complex latent distribution of the data in a Bayesian  
 418 manner improve image classification. However, for MRR the improvement is marginal and  
 419 for Accuracy@5 there even is a decrease after incorporating the spatial co-location component  
 420 because this type of spatial context falls short of taking into account the intricate *interactions*  
 421 of different context neighbors. This shortcoming is not clear when only looking at the first  
 422 few results in the ranking returned by the combined models, but it becomes clearer in later  
 423 results in the ranking output, thus resulting in a decrease for Accuracy@5 and only a slight  
 424 increase in the MRR measurement.

■ **Table 3** Accuracy@1 result using baseline models and proposed combination models using different types of spatial context and sequences

Accuracy@1	AlexNet	ResNet18	ResNet50	DenseNet161
Baseline	0.07	0.07	0.09	0.09
Relatedness	0.07	0.07	0.09	0.09
Co-location	0.15	0.17	0.17	0.17
Sequence Pattern (Random)	0.18	0.18	0.19	0.20
Sequence Pattern (Distance)	<b>0.20</b>	<b>0.20</b>	<b>0.22</b>	<b>0.22</b>
Sequence Pattern (Morton order)	0.19	<b>0.20</b>	<b>0.22</b>	<b>0.22</b>

425 The Bayesian combination model using spatial sequence patterns shows better overall  
 426 results compared with the baseline models, the spatial relatedness model, and the spatial

■ **Table 4** Accuracy@5 result using baseline models and proposed combination models using different types of spatial context and sequences

Accuracy@5	AlexNet	ResNet18	ResNet50	DenseNet161
Baseline	0.50	0.56	0.59	0.60
Relatedness	0.52	0.56	0.58	0.59
Co-location	0.42	0.44	0.45	0.44
Sequence Pattern (Random)	0.65	0.69	<b>0.73</b>	0.73
Sequence Pattern (Distance)	<b>0.67</b>	<b>0.70</b>	<b>0.73</b>	<b>0.75</b>
Sequence Pattern (Morton order)	0.65	<b>0.70</b>	0.72	0.71

427 co-location model. This is because the spatial sequence patterns capture spatial interactions  
 428 between the neighboring POIs that are neglected by the other models. From the result we  
 429 can see that using a distance-based sequence is better than using a random sequence. To  
 430 prevent confusion and to understand why the random model still performs relatively well, it  
 431 is important to remember that this model utilizes spatial context. However, it does not utilize  
 432 the distance signal within this context but merely the presence of neighboring POI. The  
 433 results show that a richer spatially explicit context, one that comes with a notion of *distance*  
 434 *decay*, indeed improves classification results. Interestingly, the sequence using Morton order,  
 435 which is widely used in geohashing techniques, does not further improve the result compared  
 436 to the distance-based sequence. There may be multiple reasons for this. First, we may have  
 437 reached a ceiling of possible improvements by incorporating spatial contexts. Second, our  
 438 Morton order implementation takes the 10 places that precede the target place in the index.  
 439 This may result in directional effects. Finally, all space filling curves essentially introduce  
 440 different ways to preserve local neighborhoods; utilizing another technique such as Hilbert  
 441 curves may yield different results. Given that the Morton order-based sequence in many  
 442 cases yield results of equal quality to the distance-based sequences, further work is needed to  
 443 test the aforementioned ideas.

444 Summing up, the results demonstrate that incorporating a (distance-based) spatial context  
 445 improves the MRR of state-of-the-art image classification systems by over **40%**. The results  
 446 for Accuracy@1 are more than **doubled** which is of particular importance for humans as  
 447 this measure only considers the first ranked result.

## 448 **6 Conclusion and Future Work**

449 In this work, we demonstrated that utilizing spatial contexts for classifying places based on  
 450 images of their facades and interiors leads to substantial improvements, e.g., increasing MRR  
 451 by over 40% and doubling Accuracy@1, compared to applying state-of-the-art computer  
 452 vision models such as ResNet50 and DenseNet161 alone. These advances are especially  
 453 significant as the classification of places based on their images remains a hard problem. One  
 454 could argue that our proposal requires additional information, namely about the types of  
 455 nearby places. However, such data are readily available for POI, and only a few nearby places  
 456 are needed. Secondly, and as a task for future work, one could also modify our methods  
 457 to work in a *drive-by-typing* mode in which previously seen places are classified, and these  
 458 classification results together with their associated classification uncertainty are used to  
 459 improve estimation of the currently seen place, thereby relaxing the need for POI datasets. In  
 460 the future, we would like to apply transfer learning and experiment with other ways to encode  
 461 spatial contexts, e.g., by testing different space-filling curves. We plan to develop models to  
 462 directly capture 2D spatial patterns rather than using a 1D sequence as a proxy and test

463 whether spatial contexts also aid in recognizing objects beyond places and their facades.

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